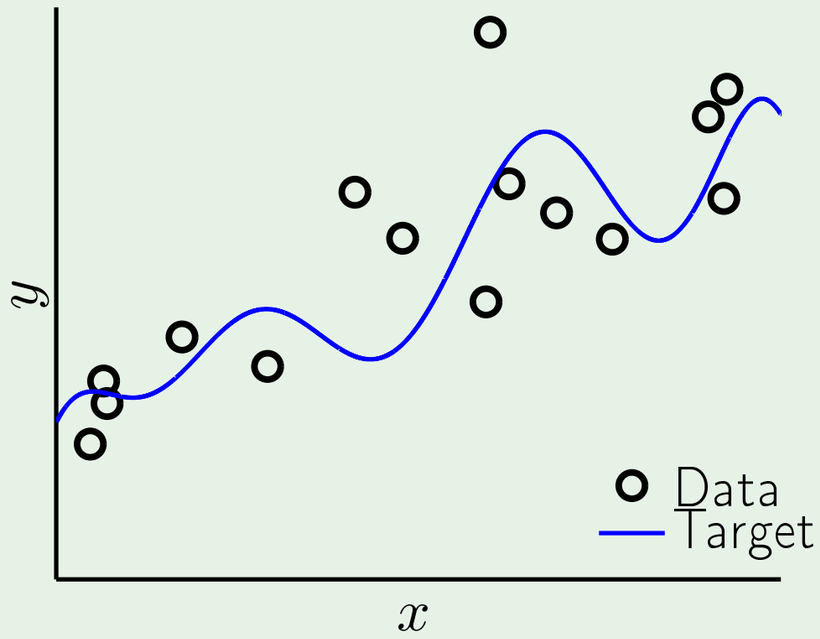
A detailed experiment

Impact of **noise level** and **target complexity**



$$y = f(x) + \underbrace{\epsilon(x)}_{\sigma^2} = \underbrace{\sum_{q=0}^{Q_f} \alpha_q \, x^q}_{\text{normalized}} + \epsilon(x)$$

noise level: σ^2

target complexity: Q_f

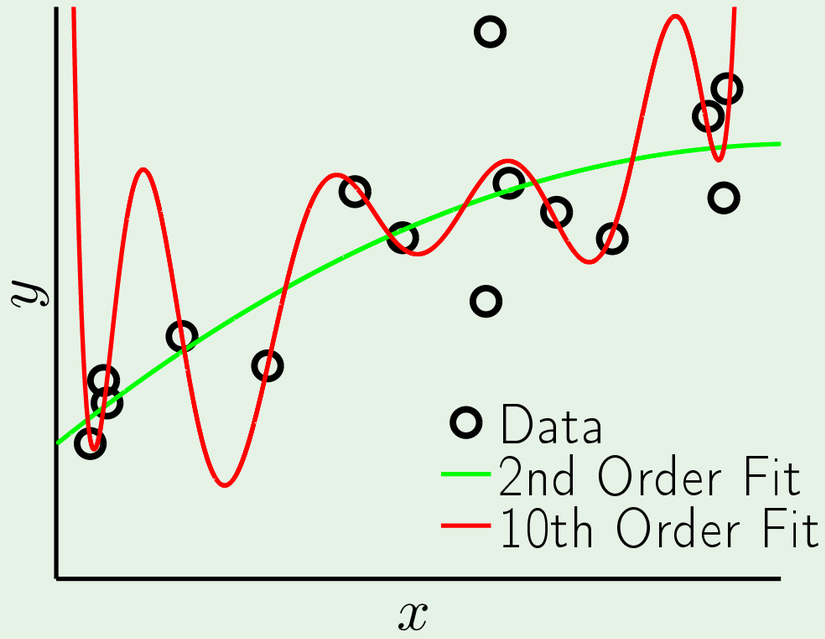
data set size: N

The overfit measure

We fit the data set $(x_1, y_1), \cdots, (x_N, y_N)$ using our two models:

$\mathcal{H}_2$: 2nd-order polynomials

$\mathcal{H}_{10}$: 10th-order polynomials

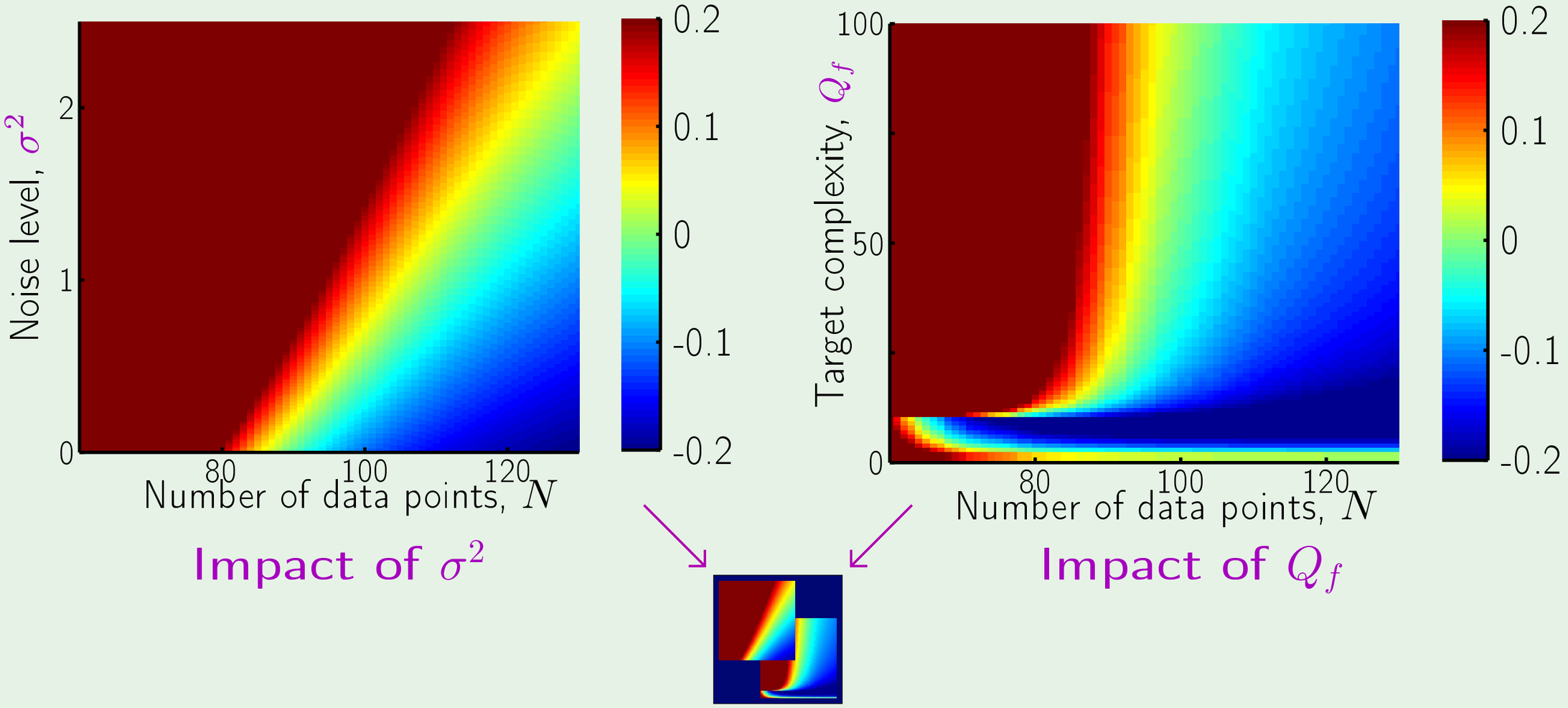


Compare out-of-sample errors of

$$g_2 \in \mathcal{H}_2 \quad \text{and} \quad g_{10} \in \mathcal{H}_{10}$$

overfit measure: $E_{\text{out}}(g_{10}) - E_{\text{out}}(g_2)$

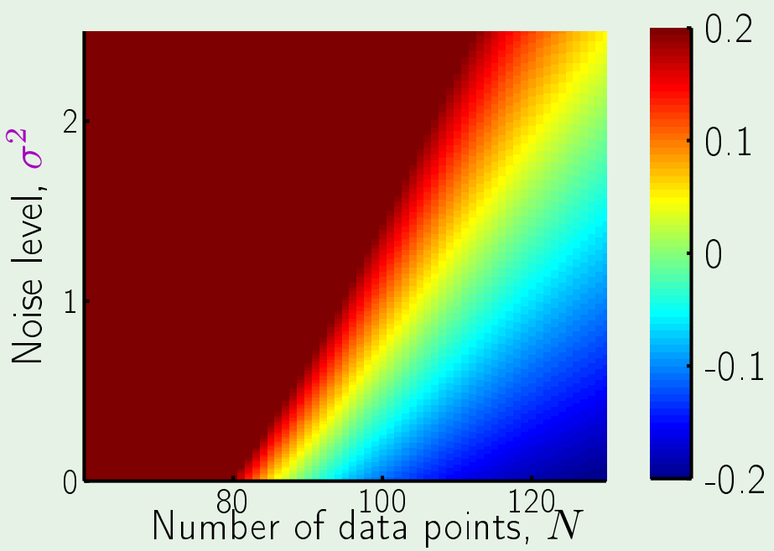
The results



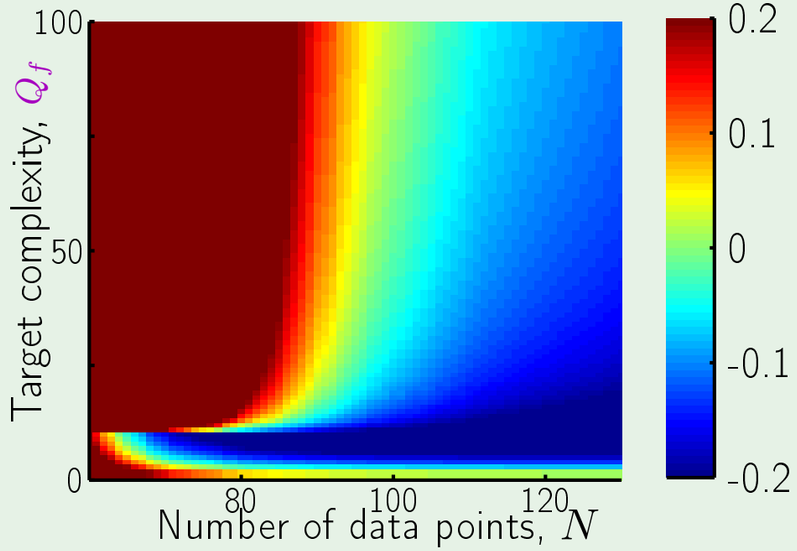
Impact of σ^2

Impact of Q_f

Impact of "noise"



Stochastic noise



Deterministic noise

number of data points	↑	Overfitting	↓
stochastic noise	↑	Overfitting	↑
deterministic noise	↑	Overfitting	↑