Example: sine target

f

$f : [-1, 1] \to \mathbb{R} \qquad f(x) = \sin(\pi x)$

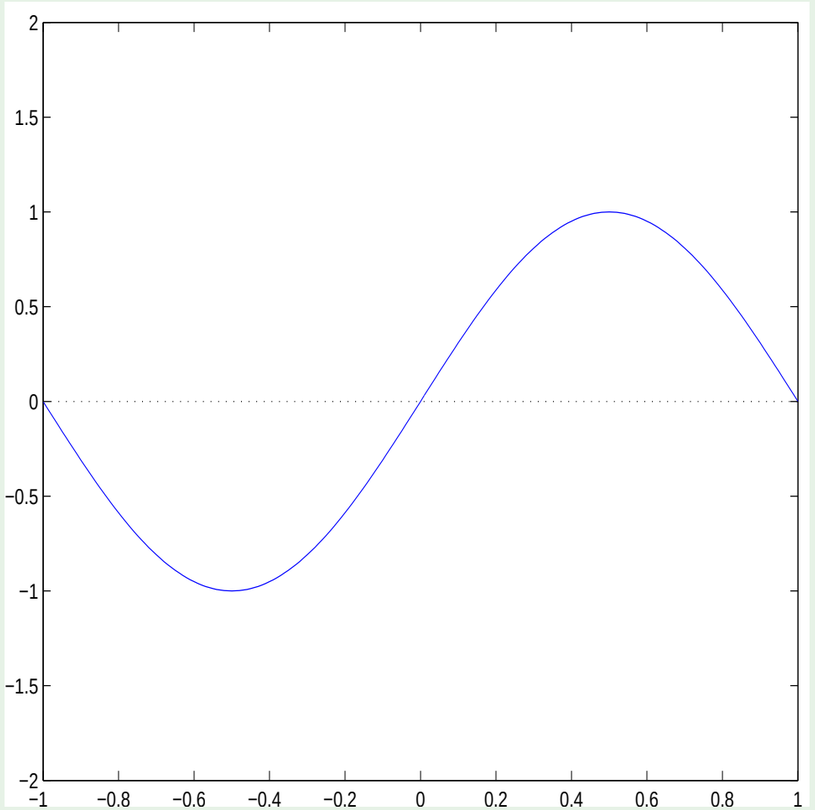
Only two training examples! $N = 2$

Two models used for learning:

$\mathcal{H}_0$: $h(x) = b$

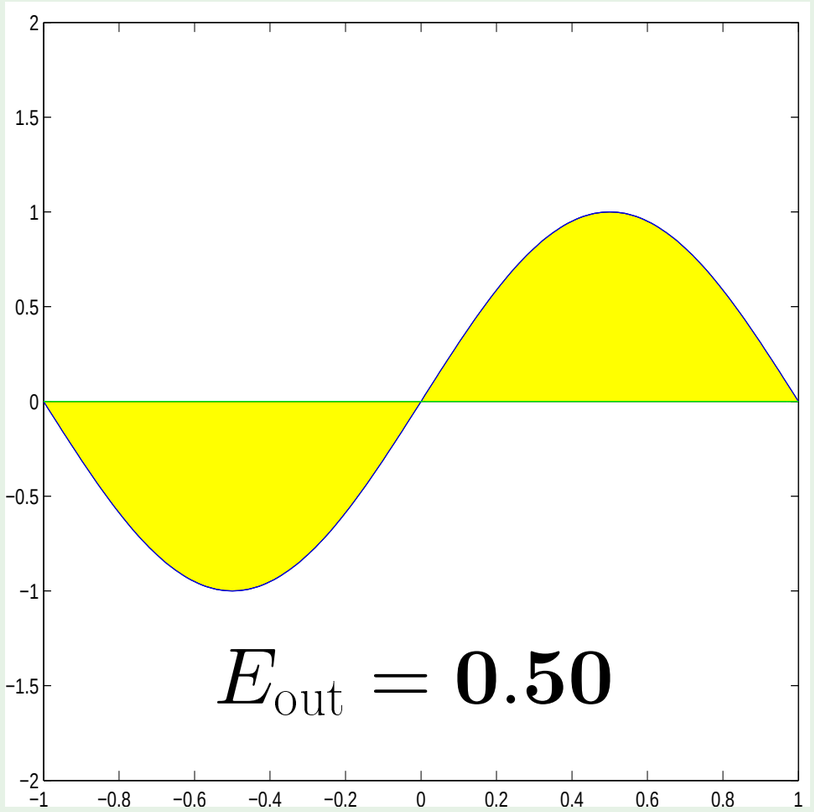
$\mathcal{H}_1$: $h(x) = ax + b$

Which is better, $\mathcal{H}_0$ or $\mathcal{H}_1$?

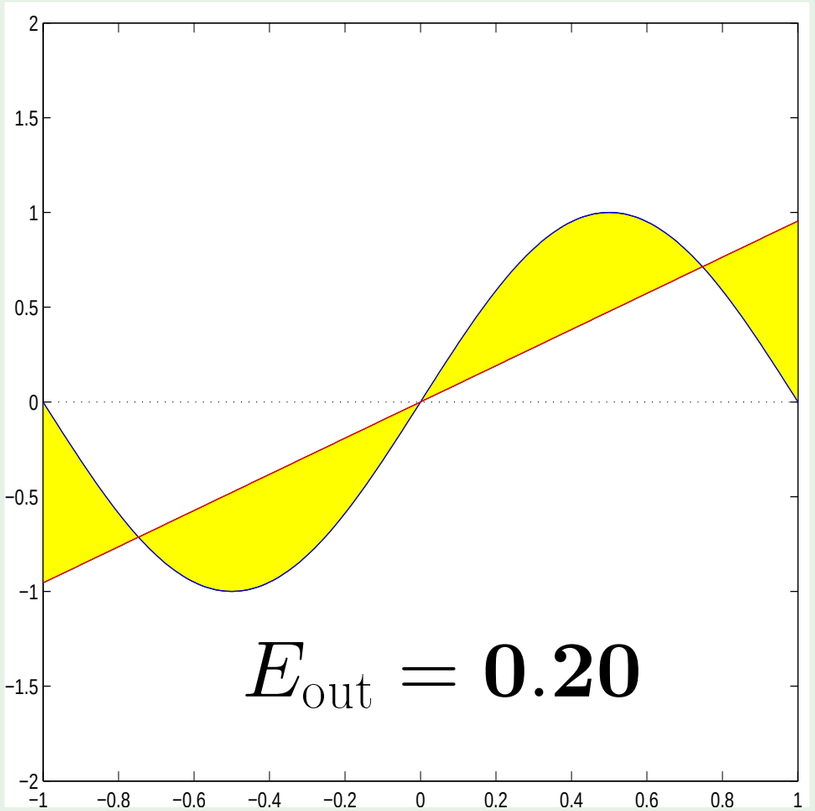


Approximation - $\mathcal{H}_0$ versus $\mathcal{H}_1$

$\mathcal{H}_0$

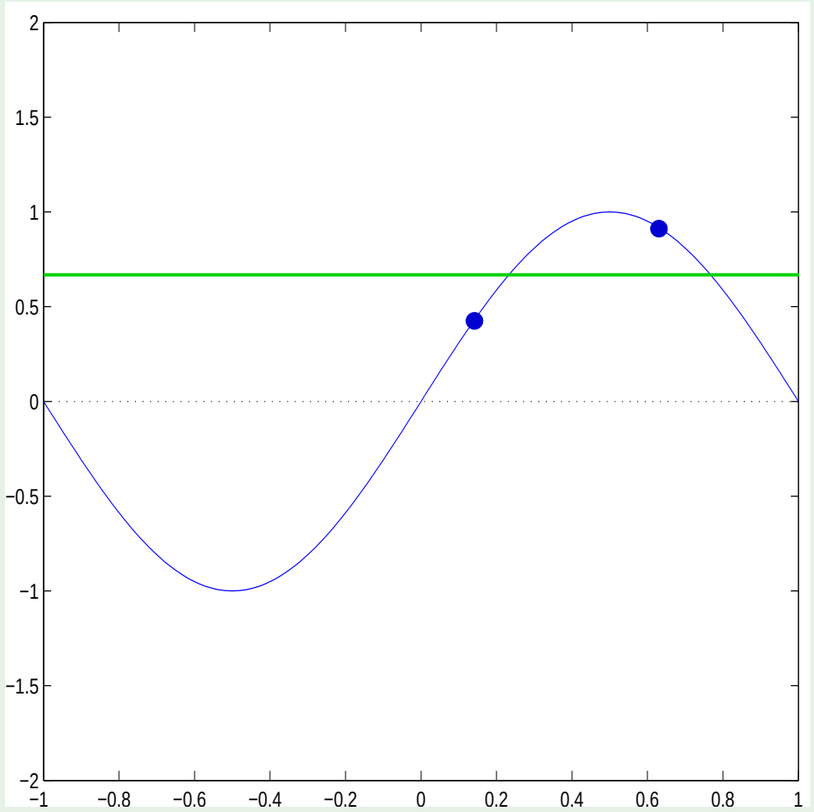


$\mathcal{H}_1$

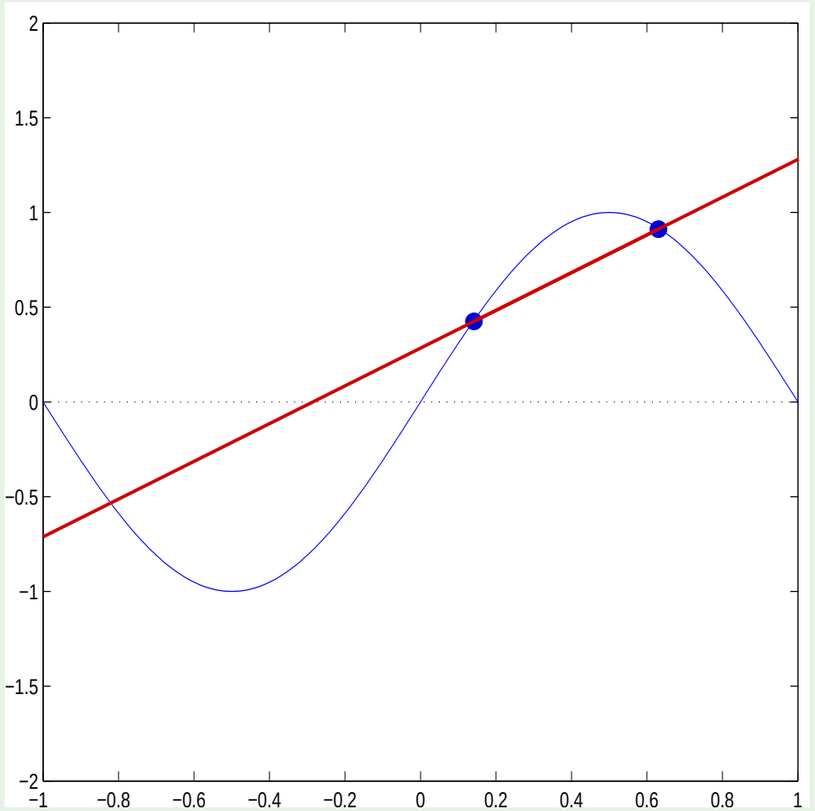


Learning - $\mathcal{H}_0$ versus $\mathcal{H}_1$

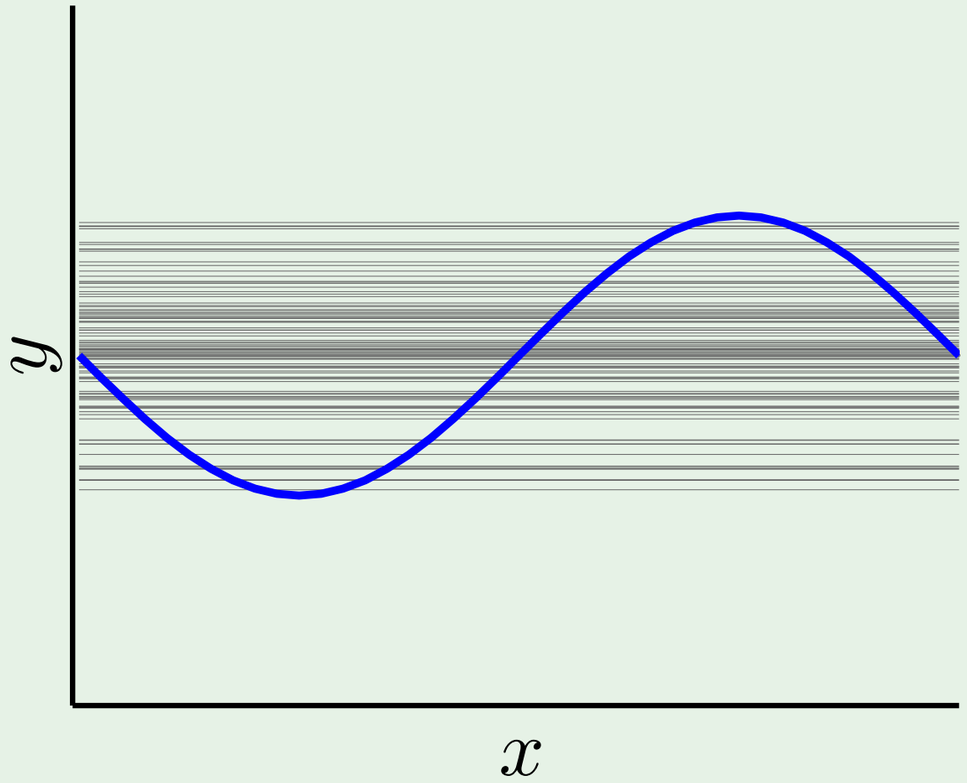
$\mathcal{H}_0$

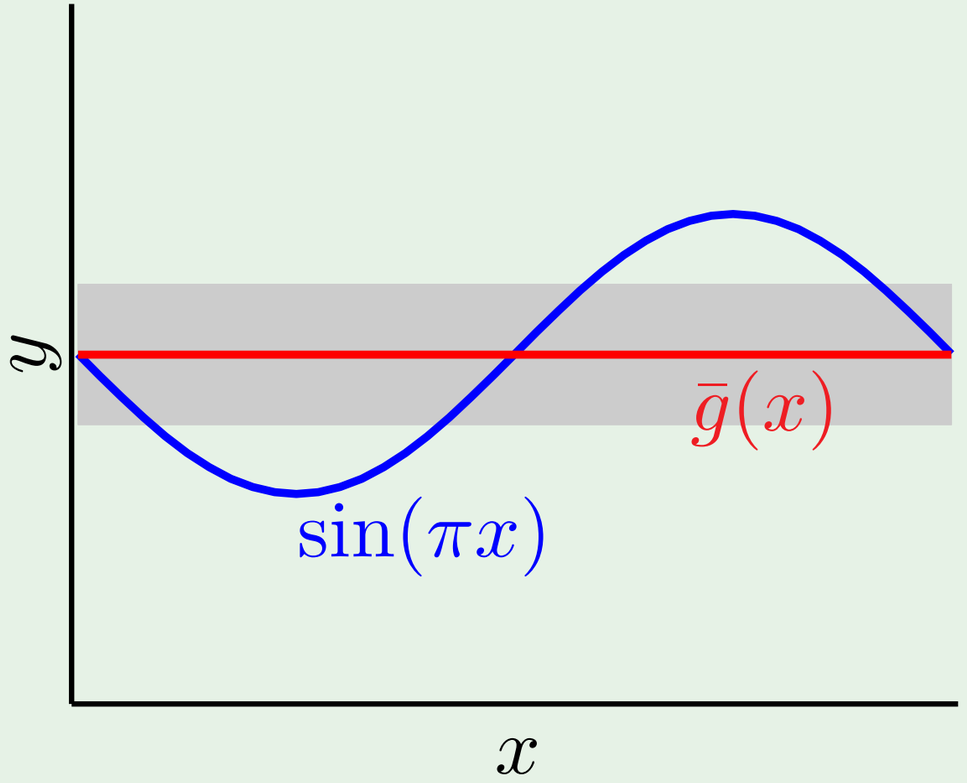


$\mathcal{H}_1$

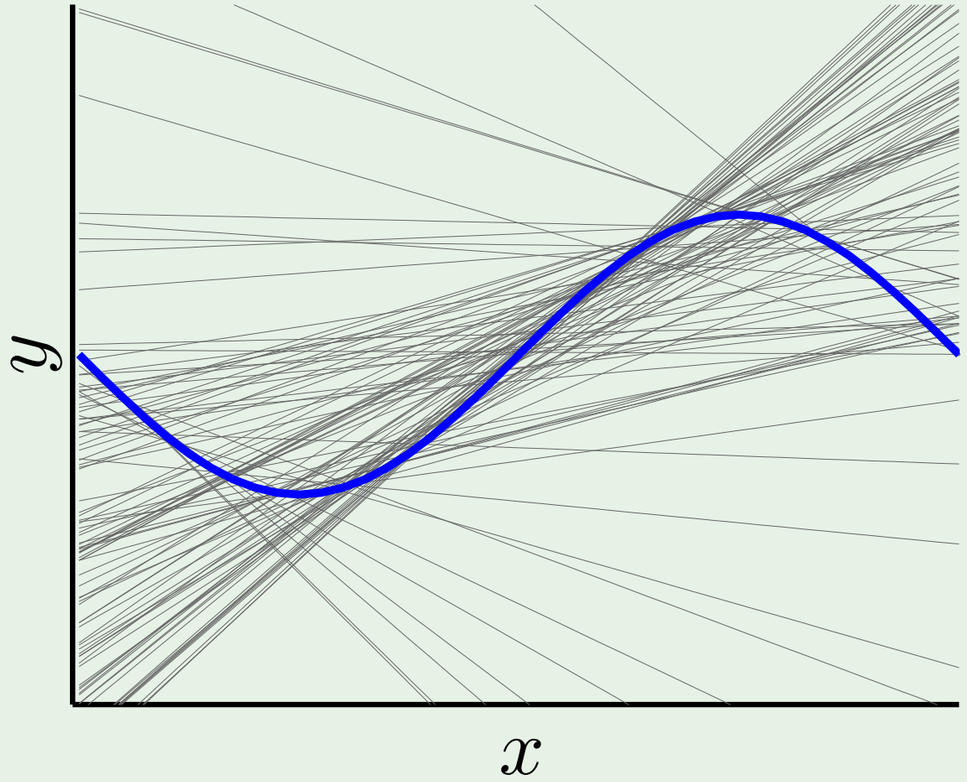


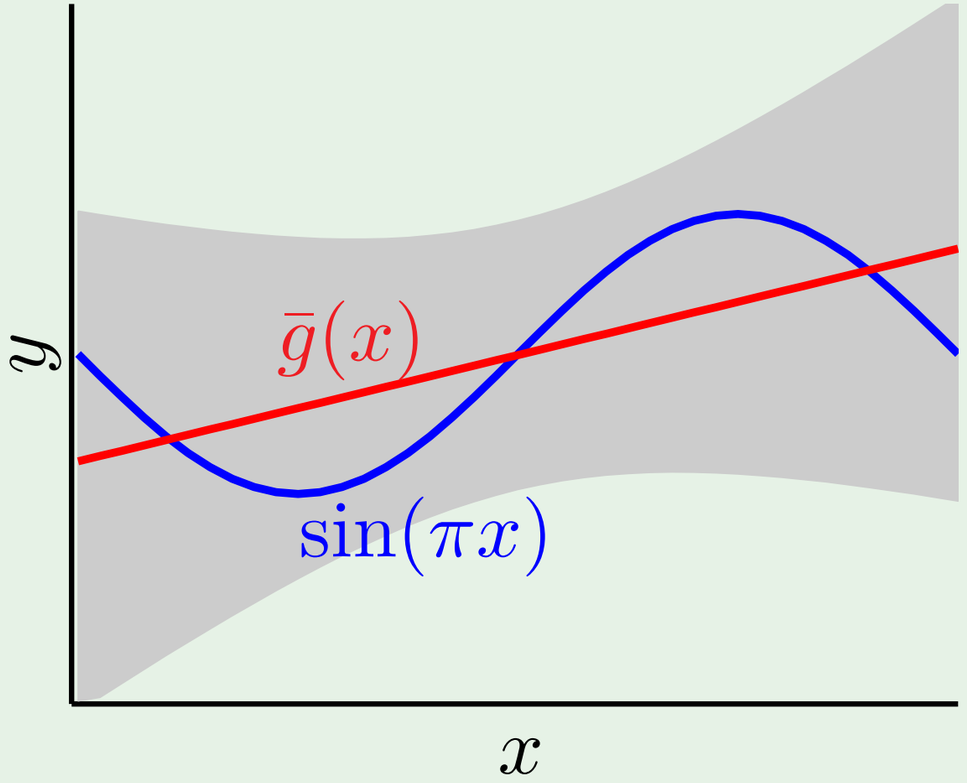
Bias and variance - $\mathcal{H}_0$



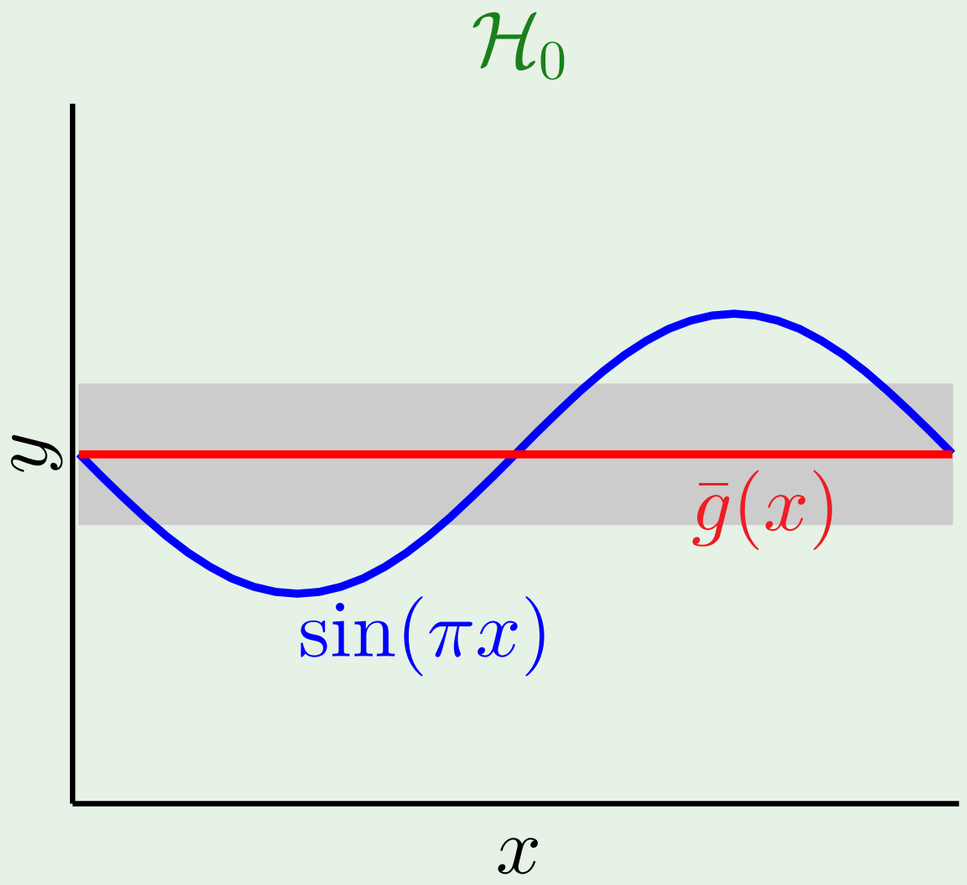


Bias and variance - $\mathcal{H}_1$

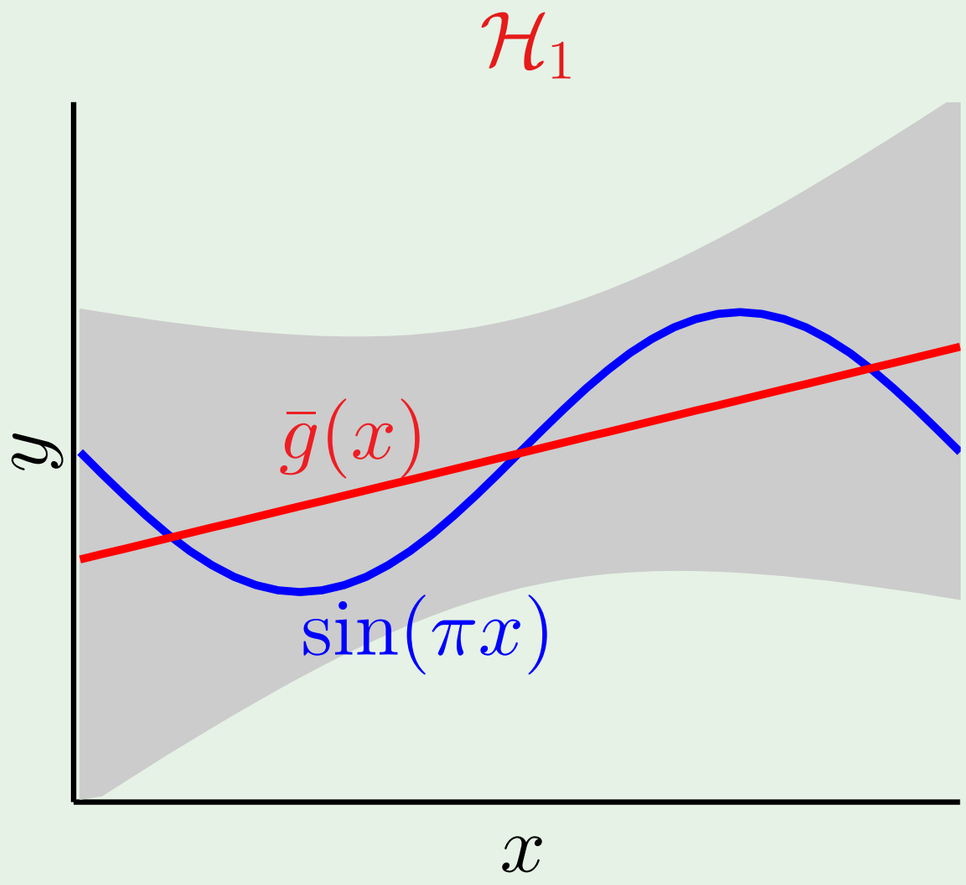




and the winner is ...



bias $= \mathbf{0.50}$ var $= \mathbf{0.25}$



bias $= \mathbf{0.21}$ var $= \mathbf{1.69}$

Lesson learned

Match the '**model complexity**'

to the **data resources**, not to the **target complexity**